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# THE REVERSE LOGISTICS MODEL WITH REUSING OF PRODUCT PARTS

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## ABSTRACT

Main goal of this paper is to create the reverse logistics model that uses reliability theory to describe reusability of product parts with assumption that recovered components are used in process of new products manufacturing. Authors assume that they aren't as good as new ones which is an important difference compared to the most models that were created before. The model allows to estimate the potential profits of the reusing policy in a production and gives the base to optimize some of the process parameters: the threshold work time of returns or the warranty period for products containing reused elements.

## 1 INTRODUCTION

Reverse logistics understood as the process of managing reverse flow of materials, in-process inventory, finished goods and related information has become one of the logicians' key areas of interest. It enjoys ever-increasing interest of many industrial branches. Nowadays a growing number of companies realize the meaning of that field of logistics. Reuse of products can bring direct advantages because company uses recycled materials or recovered components instead of expensive raw materials.

Literature survey that has been done around the theme of the reverse logistics area, allowed to set out this article aims and objectives. In the reverse supply chain the issue of: timings, quantities and conditions of returned and reusable components make production planning difficult (Murayama et al., 2006). The majority of models assume that demand for new products and returns quantity are independent Poisson random variables (Plewa & Jodejko-Pietruczuk, in prep.) and very few use the reliability theory to estimate the number of reusable products. Murayama et al. (Murayama et al., 2001, 2005, 2006) propose the method to predict the number of quantities of returned products and reusable components at each time period by using series system reliability models. The condition aspect of returns in a reverse logistic system is usually omitted by using assumption that all the returns are reusable and usually "as good as new" (e.g. Kiesmüller, 2003). Only few models use the reliability theory to diversify returned elements' reusability, but they don't give any guidelines for the way to optimize the threshold value of components' residual life (e.g. Murayama et al., 2001, 2005, 2006).

Literature review that have been done so far, allowed to define the main shortages of existing logistics models that deal with the reverse logistics problem:

- most of the created models assume single-component product,
- they are based on the assumption that recovered products are as good as new,
- they don't optimize reusability of the returns.

Main goal of this paper is to create the reverse logistics model that uses the reliability theory to describe reusability of product parts with assumption that recovered components are used in a production process but they aren't as good as new ones. The model allows to estimate the potential profits of the reusing policy in a production and gives the base to optimize some of the process parameters: the threshold work time of returns or the warranty period for products containing reused elements.

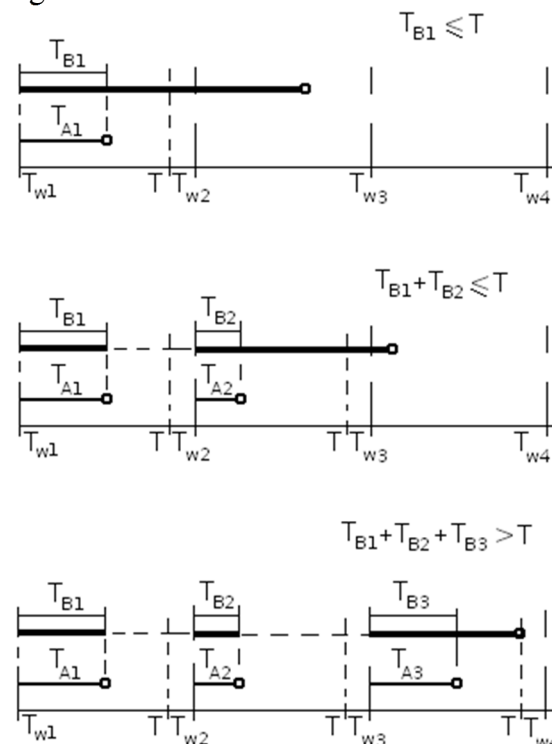
## 2 THE MODEL OF THE REUSING POLICY

The model that is presented in the paper is based on the following assumptions:

- A company produces the object composed of two elements (A and B). The product fails when one of components fails – series reliability structure.
- A failure of each component occurs independently on other components' failures.
- If the product fails during the warranty period, it is returned to the manufacturer and he has to pay some penalty cost (e.g. the cost of a new product).
- The products are returned as soon as their lives are ended.
- The component B of the product may be reused in a new production, if it was not the cause of a product failure and its total work time up to this moment is not greater than some acceptable – threshold time  $T$  (Fig. 1).
- Neither failed elements B can be reused in a new production (not repairable) nor any A element. All A components are new in a new production.
- Demand for the products is determined.
- New products are manufactured and sold in established moments (for simplicity – at the beginning of every warranty period).

The process of reusing of the component B, dependently on its threshold age  $T$ , is shown in Figure 1.

Despite the fact that companies realize the potential of reusing products, the question “is it worth to do it”, is not so simple to answer. Within main reasons for products reusing are: difficulties with raw material supplying, high cost of utilization of returned and damaged products or lower cost of reusing of products' components than buying new ones. The objective of the presented model is to estimate profitability of using returned and recovered elements in a new production, in the case when they are not as good as new.



**Figure 1.** Process of element reusing in a new production.

According to above assumptions, before every production beginning, the manufacturer has to make the decision: which of returned elements B should be used in the new production. The usage of recovered components decreases production costs but also increases the risk that additional costs occur because of larger amount of returns during the warranty period. The objective is to find the threshold work time  $T$  for returned element that equalizes potential cost and profits of the reusing policy:

$$E(C_{WO}(T_W, T)) - E(C_{WN}(T_W, T)) = C_B - C_R - C_M \quad (1)$$

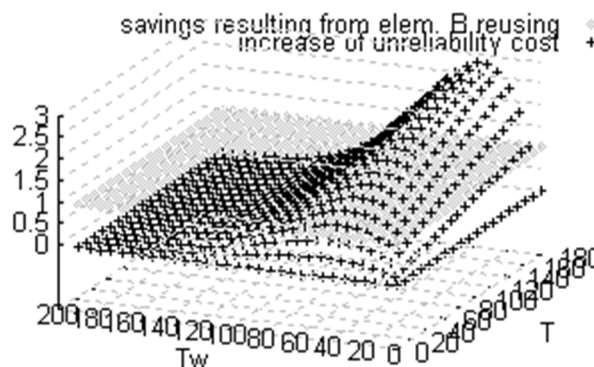
$$E(C_{WO}(T_W, T)) = \left[ 1 - \frac{R_B(T_W + T)R_A(T_W)}{R_B(T)} \right] C_O \quad (2)$$

$$E(C_{WN}(T_W, T)) = [1 - R_B(T_W)R_A(T_W)]C_O \quad (3)$$

where  $C_{WO}$  = the cost of warranty services if an “old” element is used in a new production;  $T_W$  = the warranty period of the product;  $T$  = the threshold age of the element B, after that the further exploitation isn't continued;  $C_{WN}$  = the cost of warranty services if a “new” element is used in production;  $C_B$  = the purchase cost of a new element B;  $C_R$  = the total cost of all activities of: decomposition, cleaning, preparing of the returned B element to reusing in a production;  $C_M$  = the cost of elements' identification;  $C_O$  = penalty cost resulting from a product failure during warranty period (e.g. the total cost of production of a new object);  $R_A(t)$  = reliability of the element A in  $t$  moment;  $R_B(t)$  = reliability of the element B in  $t$  moment;  $E(x)$  = the expected value of variable  $x$ .

The left side of the equation 1 specifies the increase in expected costs of product warranty services (during a single warranty period) caused by the reusing in a production element that is not as good as new. This part of the expression depends on: both elements' reliability (A and B), the length of warranty period and the length of the acceptable total work time  $T$  of the returned B element. The direction of changes in the expected cost of reusing elements is not so obvious. In special cases (low value of time  $T$  and short warranty period) it can happen that reused product is more reliable than a new one. The right side of the equation 1 determines the potential cost savings resulting from using cheaper, recovered components instead of new elements.

On the basis of this expression you can find the threshold value  $T$  of total work time of the element B, above which reusing the component is not economical. An analytical solution of the equations can't be achieved for the majority of probability distributions describing components' time to failure, but the value of  $T$  can be easily found by applying numerical calculations for given vector of  $T$ . The example of numerical analysis of the equation 1 is presented in Figure 2.



**Figure 2.** Increase of unreliability costs and savings resulting from the reusing policy for various values of threshold work time ( $T$ ) and warranty periods ( $T_w$ ) for process parameters:  $c_O = 5$ ,  $c_B = 1$ ,  $c_R = c_M = 0$ ,  $R_A = R_B = \exp(-(t/100))^2$ .

This way, for given warranty period, you can find the threshold total work time  $T$ , for which using returned element B is economical (costs are lower than savings). It is interesting that for very long warranty periods (longer than double expected lifetime of the product) reusing elements is still profitable. It is an obvious effect of a very low product reliability in the whole warranty time and even using “old” components can't deteriorate it.

### 3 MODEL DEVELOPMENT

The practical application of the presented model is limited, because it calculates potential profits and costs assuming that all elements used in a new production are in the age of  $T$ . Monte Carlo simulation that was built to compare analytical and numerical results showed that this simplified assumption deforms real values of cost and benefits of components' reusing.

According to previous assumptions, at every moment of production beginning the producer has to make the decision: which of returned elements B should be used in the production. The threshold work time  $T$  (for which savings from components' reusing are equal losses) can be specified on the base of Equation 1, but practical questions require more precise data: how many reusable elements will return before the new production batch, how many new components must be kept in a stock or what is the expected profit/cost when mix of new-old elements will be used in the production.

To answer this questions, the model should consider the percent of returns used in the production:

$$n = (1 - R_A(\min(T, T_W))) R_W(\min(T, T_W)) \quad (4)$$

where  $n$  = production batch percent of reusable B elements, that return during warranty period;  $T_W$  = the warranty period of the product;  $T$  = the threshold age of the element B, after that the further exploitation isn't continued;  $R_A(t)$  = reliability of the element A in  $t$  moment;  $R_B(t)$  = reliability of the element B in  $t$  moment;  $\min(x, z)$  = minimum value of variables  $x$  and  $y$ .

Real values of costs and savings coming from the reusing policy is proportional to the variable  $n$ :

$$\left[ E(C_{WO}(T_W, T)) - E(C_{WN}(T_W)) \right] n = (C_B - C_R)n - C_M \quad (5)$$

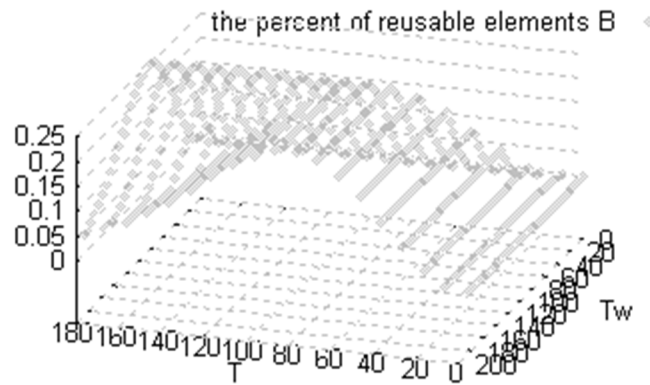
where  $C_{WO}$  = the cost of warranty services if “old” element is used in a new production;  $T_W$  = the warranty period of the product;  $T$  = the threshold age of the element B, after that the further exploitation isn't continued;  $C_{WN}$  = the cost of warranty services if “new” element is used in a production;  $n$  = production batch percent of reusable B elements, that return during warranty period;  $C_B$  = the purchase cost of a new element B;  $C_R$  = the total cost of all activities of preparing of returned B element to reusing in a production;  $C_O$  = penalty cost resulting from a product failure during warranty period;  $E(x)$  = the expected value of variable  $x$ .  $C_M$  = the cost of elements' identification, it is independent on the number of returns, because if a company decides to apply the reusing policy, all elements used in a production have to be identified.

### 4 RESEARCH RESULTS

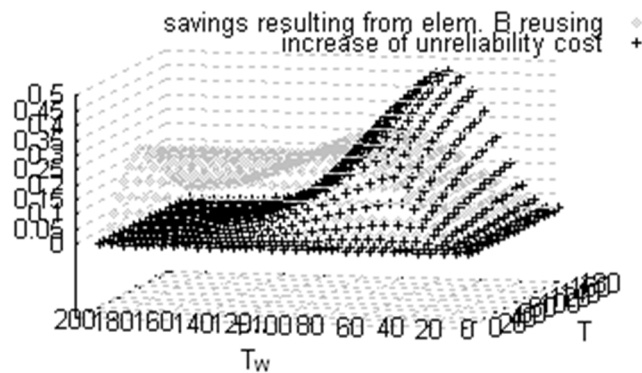
The process of planning, implementing, Some example of analytical model and simulation results are presented in figures 3-7 (for process parameters:  $C_O = 5$ ,  $C_B = 1$ ,  $C_R = C_M = 0$ ,  $R_A = R_B = \exp(-(t/100))^2$ ). The results are obtained for the same process parameters as in Figures 2, but are different than previous ones because of the influence of returned elements amount, used in a new production batch.

Savings coming from element reusing in Figure 2 are constant for all analysed values of  $T$  and  $T_w$ , but they have irregular shape in Figure 4. Considering two alternative values of the total work time  $T$ , sometimes it is more economical to get lower unit profit but coming from greater quantity of reused elements.

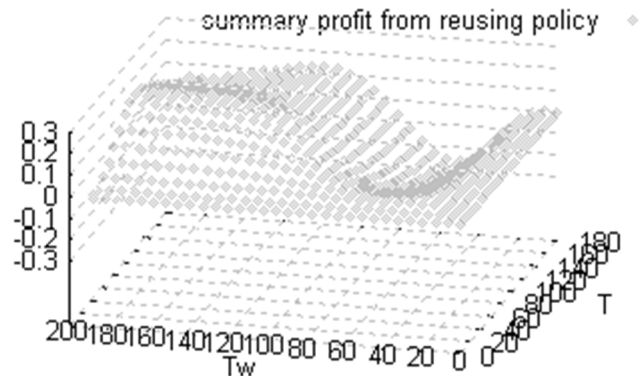
Figure 5 presents the summary profit resulting from reusing of elements in new production. The profit sometimes gets values lower than zero because losses of components' reusing are higher than potential savings. Irregular shape of reusing policy benefits and costs shows that plane may have more than one local maximum or minimum. The research conducted for various process parameters haven't given any general rules where the optimal value of work time  $T$  may be found.



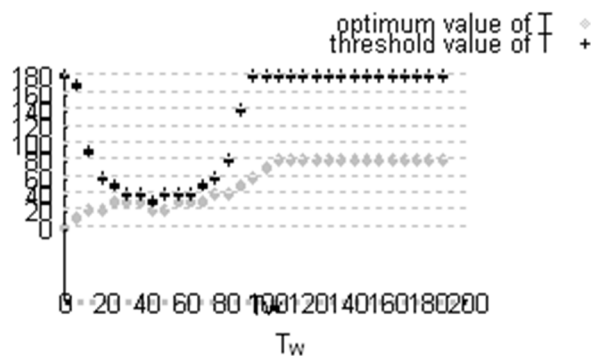
**Figure 3.** Production batch percent of reusable B elements, that may be used in new production.



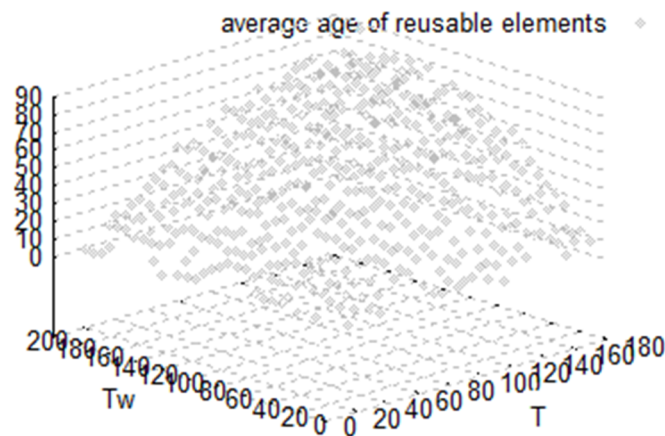
**Figure 4.** Savings and losses resulting from reusing of elements B in new production.



**Figure 5.** Summary profit resulting from reusing of elements B in new production.



**Figure 6.** Optimum value of  $T$  (saving resulting from the reusing policy gets maximum) and threshold value of  $T$  (reusing is not economical above this value).



**Figure 7.** Average age of reusable elements

Figure 7 presents the average age of returned elements that can be reused in a new production, obtained during simulation experiments. The age usually is equal approximately 0,4 – 0,6 of the shorter value: warranty period or threshold work time  $T$ .

## 5 SENSITIVITY ANALYSIS

In order to assess the influence of the reusing process parameters on its cost results, the sensitivity analysis of the proposed model was conducted. The parameters that was concerned as the most meaningful were tested and the results obtained during the research are shown in Figures 8-15.

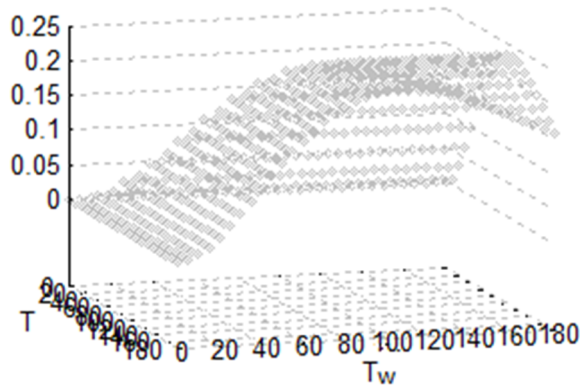
When a returned component that was working some time in the past is used in the product offered as new for a customer, the element's intensity of failures is one of the determinant of possible reusing. For this reason the impact of the reusable component failure rate on production process costs and profit was tested.

Exponentially distributed time to failure has a constant failure rate and reusing of such elements always is profitable (Fig. 8,11). The optimal value of work time  $T$ , for which the profit is the highest, gets maximum possible value for all tested warranty periods (Fig. 12). The sudden decrease in optimal  $T$  value for warranty periods two times longer than co-component's (A) expected time to failure is the effect of lower number of possible returns of the product. Only in the

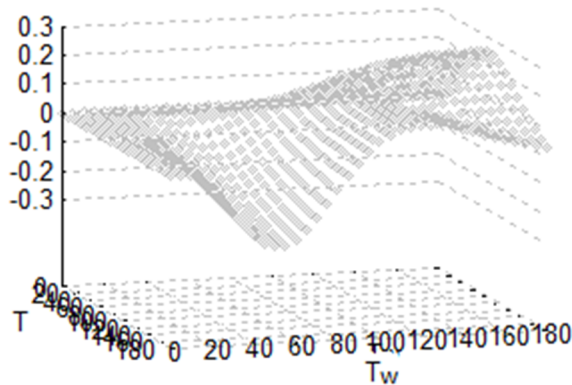
case when A element fails during a warranty period and is returned to the manufacturer, reusing of B components is possible. The optimum  $T$  takes value of double A lifetime.

Figures 9,10 present cost results of the reusing policy for the growing failure rate of the reusable component. The faster growth of this parameter shifts the threshold and the optimal  $T$  to lower values – reusing is less profitable (Fig. 11,12).

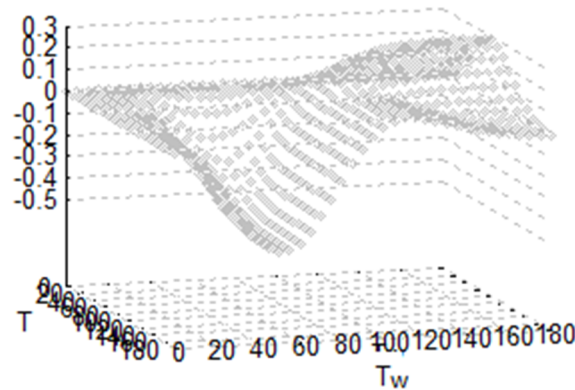
The second most meaningful parameter of the reusing process is the relationship between possible costs of warranty services and savings coming from the lower number of elements in the production process. The research results are presented in Figures 13-15. They are quite obvious – higher cost of a product failure during warranty period causes lower profitability of reusing policy.



**Figure 8.** Summary profit resulting from reusing of elements B in new production for  $C_O = 5, C_B = 1, C_R = C_M = 0, R_A = \exp(-(t/100))^2, R_B = \exp(-(t/100))^1$ .

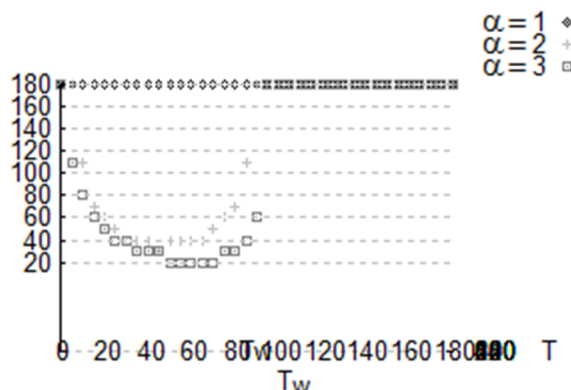


**Figure 9.** Summary profit resulting from reusing of elements B in new production for  $C_O = 5, C_B = 1, C_R = C_M = 0, R_A = \exp(-(t/100))^2, R_B = \exp(-(t/100))^2$ .

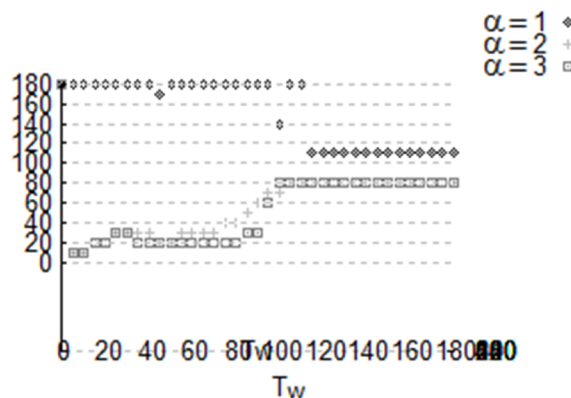


**Figure 10.** Summary profit resulting from reusing of elements B in new production for  $C_O = 5, C_B = 1, C_R = C_M = 0, R_A = \exp(-(t/100))^2, R_B = \exp(-(t/100))^3$ .

The shape of threshold values of  $T$  time may also be interesting (e.g. Fig.11,14). For very short warranty periods the costs are usually equal to the saving and are very close to zero. It is the effect of very low changes of reliability of the product in very short time. In such cases reusing even “very old” (high values of threshold time  $T$ ) component is profitable.

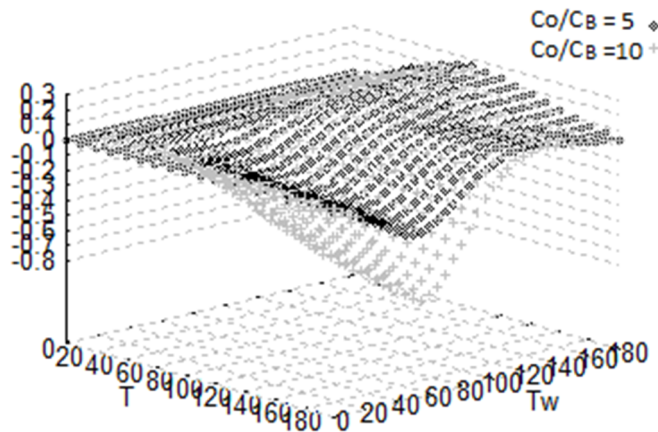


**Figure 11.** Threshold value of  $T$  for  $C_O = 5, C_B = 1, C_R = C_M = 0, R_A = \exp(-(t/100))^2, R_B = \exp(-(t/100))^3$ .

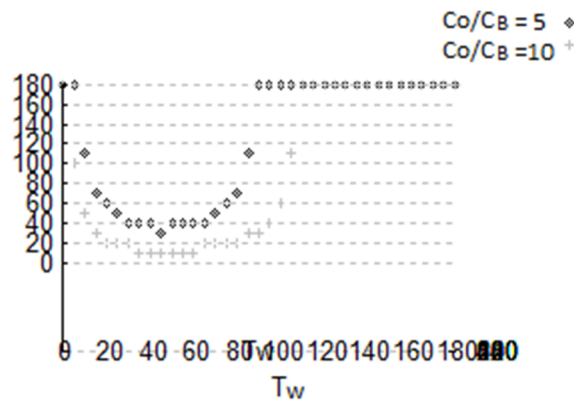


**Figure 12.** Optimum value of  $T$  for  $C_O = 5, C_B = 1, C_R = C_M = 0, R_A = \exp(-(t/100))^2, R_B = \exp(-(t/100))^3$ .

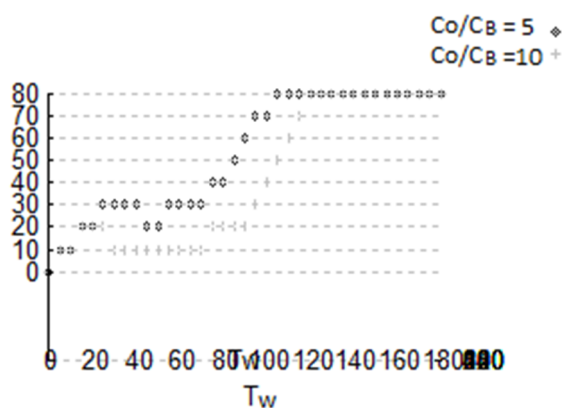




**Figure 13.** Summary profit resulting from reusing of elements B in new production for  $C_O = 5$  and  $C_O = 10$ ,  $C_B = 1$ ,  $C_R = C_M = 0$ ,  $R_A = \exp(-(t/100))^2$ ,  $R_B = \exp(-(t/100))^2$ .



**Figure 14.** Threshold value of  $T$  for  $C_O = 5$  and  $C_O = 10$ ,  $C_B = 1$ ,  $C_R = C_M = 0$ ,  $R_A = \exp(-(t/100))^2$ ,  $R_B = \exp(-(t/100))^2$ .



**Figure 15.** Optimum value of  $T$  for  $C_O = 5$  and  $C_O = 10$ ,  $C_B = 1$ ,  $C_R = C_M = 0$ ,  $R_A = \exp(-(t/100))^2$ ,  $R_B = \exp(-(t/100))^2$ .

## 6 CONCLUSIONS

The model presented in this paper is the continuation of wide researches in the reverse logistics area. The majority of models deal with single – element system or with the assumption that

reused elements are as good as new. The proposed model develops the previous ones by releasing both assumptions and gives the base to determine some of reusing policy parameters such as: the threshold work time of re-turned element that can be used again, the warranty period for the product containing elements which have some history of work, the size of new elements' stock necessary to fulfill production planes. The model is presented and tested for two-element, series system but it is very simple to be developed it to the case of x-element, series system. From the point of view of possible product returns during a warranty period this assumption is usually real because only a failure of a one product component allows to reuse others.

Although the majority of presented expressions is difficult to solve analytically, their analytical form enables easy implementation to a numerical search of optimal process parameters.

Effects of the analytical calculations of the presented model were confirmed and fulfilled by simulation results but it is obvious that the model should be verified in practice.

Practical application of the model is possible in companies which are interested in the reusing policy because the decision must be supported by the calculation of possible cost and benefits. Further development of the model should release the assumptions about deterministic demand for the product and constant moments of production.

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